$$(2D-4)(x)-(D-2)(y)=4e^{2x}$$

$$(D+7)(x)+(2D-1)(y)=-5e^{-2x}$$

$$(D+7)(2D-4)(x)-(D+7)(D-2)(y)=-6e^{-2x}+28e^{-2x}=20e^{-2x}$$

$$(2D-4)(D+7)(x)+(2D-4)(2D-1)(y)=-20e^{-2x}+20e^{-2x}=40e^{-2x}$$

$$(2D-4)(D+7)(x)+(2D-4)(2D-1)(y)=-20e^{-2x}+20e^{-2x}=40e^{-2x}$$

$$(D^2-D-2)(y)=-4e^{-2x}$$

$$(D^2-D-2)(y)=-4e^{-2x}$$

$$y=-2e^{-2x}+2e^{-2x}$$

$$y=-2e^{-2x}+2e^{-2x}$$

$$y=-2e^{-2x}+2e^{-2x}$$

$$y=-2e^{-2x}+2e^{-2x}$$

$$y=-2e^{-2x}+2e^{-2x}$$

$$(D-2)(y)=-16e^{-2x}+2e^{-2x}=-20e^{2x}$$

$$(D-2)(y)=-16e^{-2x}+10e^{-2x}=-20e^{2x}$$

$$(D-2)(y)=-16e^{-2x}+10e^{-2x}=-20e^{2x}$$

$$(D-1)(x)=0$$

$$x=-2e^{2x}+2e^{-2x}$$

$$(D-1)(x)=0$$

$$x=-2e^{-2x}$$

$$(D-1)(x)=0$$

$$(D-1)(x)=0$$

$$(D-1)(x)=0$$

$$(D-1)(x)=0$$

$$(D-1)(x)=0$$

$$(D-1)($$

y=-xcosx-xsmx-x-1+Acosx+Bsinx+Cex

 $y = e^{-2x}$  is a solution of the homogeneous differential equation (2x+1)y'' + 4xy' - 4y = 0.

SCORE: \_\_\_\_\_/ 40 PTS

Find the general solution of the non-homogeneous differential equation  $(2x+1)y'' + 4xy' - 4y = 2e^{-2x}(2x+1)^2$ .

$$y_{1}^{z} = V^{2-2x}$$

$$y_{1}^{y} = V^{y} = 2x = 2ve^{2x}$$

$$y_{2}^{y} = V^{y} = 2x = 4v^{y} = 2x + 4ve^{2x}$$

$$e^{2x} \left[ v''(2x+1) + v'(-4(2x+1)) + v(4(2x+1)), (3) + v'(-4x) \right] = 0$$

$$+ v'(-4x) = 0$$

$$+ v'(-4x) = 0$$

$$- v'(-4$$

 $y = 4\sqrt{x}$  is a particular solution of the non-homogeneous differential equation  $9x^2y'' - 3xy' + 4y = \sqrt{x}$ . SCORE: \_\_\_\_\_/ 15 PTS Solve the initial value problem  $9x^2y'' - 3xy' + 4y = 2\sqrt{x}$ , y(1) = -7, y'(1) = 5.